**ARCHIVES OF ELECTRICAL ENGINEERING** 

VOL. 72(1), pp. 211 -228 (2023)

DOI 10.24425/aee.2023.143698

# A comparative study based on proportional integral and backstepping controllers for doubly fed induction generator used in wind energy conversion system

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(Received: 11.04.2021, revised: 09.11.2022)

**Abstract:** This paper presents a comparative study between the conventional PI (Proportional Integral) and backstepping controllers applied to the DFIG (Doubly Fed Induction Generator) used in WECS (Wind Energy Conversion System). These two different control strategies proposed in this work are developed to control the active and reactive power of the DFIG on the one hand, and to maintain the DC-link voltage constant for the inverting function on the other hand. This is ensured by generating control signals for two power electronic converters, RSC (Rotor Side Converter) and GSC (Grid Side Converter). In order to optimise the power production in the WT (Wind Turbine), an MPPT (Maximum Power Point Tracking) algorithm is applied along with each control technique. To simulate the effectiveness of the proposed controllers, MATLAB/Simulink Software is used, and the obtained results are analysed and discussed to compare PI and backstepping controllers in terms of robustness against wind speed variations and tracking performance in dynamic and steady states.

Key words: backstepping control, control, DFIG, GSC, MPPT, PI, RSC, wind turbine

#### 1. Introduction

The huge increase in energy needs and demands around the world forces the international community to invest more in renewable energy sources [1]. This shift towards renewable energies makes wind energy become one of the fastest growing and most reliable renewable energy technologies, especially in the last few decades [2, 3]. In this context many studies have been



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conducted in attempt to enhance the efficiency of the wind turbines as well as to improve the quality of the energy produced.

Most of WTs (Wind Turbines) that are installed nowadays are based on variable speed generators, the DFIG (Doubly Fed Induction Generator) [4, 5]. It is the most used generator, especially in conventional gear-driven WT systems due to its several advantages such as the small size of the converters needed for power control as they are penetrated only by a fraction of the rated power. It's also more useful to control power in case of high wind speed for protection reasons. Another advantage is that the DFIG does not need either a reactive power compensator or a soft starter because its structure offers the possibility to control reactive power exchanged between the turbine and the grid through two electronic converters, the RSC (Rotor Side Converter) and GSC (Grid Side Converter) [6].

The most typical topology design of the WECS (Wind Energy Conversion System) is shown in Fig. 1, where the turbine shaft drives the rotor of the DFIG through the gear box system. The stator windings are directly connected to the power grid whereas the rotor windings are connected to the grid through back-to-back power electronic converters, the RSC and GSC, with a DC-link capacitor in between to keep the voltage constant for the inverting function [4,6].

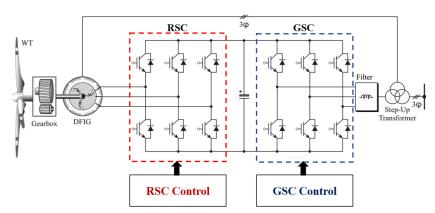


Fig. 1. Block diagram of WECS based on DFIG

In order to maximise the power captured by the WT, the control strategy of the DFIG has become the issue and interest of recent studies as highlighted by F. Mohammadi *et al.* [7].

In a grid connected wind turbine, power fluctuations have a negative effect on the quality of energy produced. To deal with this issue some studies propose an optimal control method in order to optimise the capacity and reliability of storage devices [8]. The use of emergency power transmission lines is also proposed despite the economic uncertainties [9].

The most popular strategy adopted to control the WT is the conventional PI (Proportional Integral) but the non-linearity of the DFIG makes it difficult to achieve satisfying performances in terms of reference tracking and speed response. That is why we propose a non-linear controller based on a backstepping approach to be applied to both converters, to consider the useful non-linearities of the system [10].

Furthermore, a detailed comparative study between the PI and backstepping controllers will be presented in this article to test their performances in terms of robustness against wind speed variations and reference tracking in dynamic and steady states.

This paper is organised as follows:

In section 2, the related work is given. Section 3 gives the dynamic model of the WECS including the DFIG. A PI controller is designed in section 4, a backstepping controller is developed in section 5. Simulation results are presented and discussed in section 6. Finally, section 7 contains the conclusion.

#### 2. Related work

The literature review shows that there is a series of studies that contributed to the design of PI and backstepping control strategies applied to the DFIG driven by the WT.

- El Mouhi *et al.* [11] proposed an active and reactive power control of the DFIG used in the WECS using the PI controller and backstepping. This study focused on the difference between PI and backstepping controllers in terms of dynamic response.
- M. Nadour *et al.* [12] proposed a comparative analysis between PI and backstepping control strategies of the DFIG driven by the WT. This study shed the light on the comparison in terms of parametric variations.
- S. Mensou *et al.* [13] proposed the backstepping controller for a Variable Wind Speed Energy Conversion System based on the DFIG. In this study, the backstepping control performance has been evaluated against random speed variations.
- A.J. Laafou proposed the dynamic control of the DFIG used in wind power production, based on a PI regulator. In this work the performances of the PI controller are simulated and tested [11].
- Y. Moumani *et al.* [15] proposed modeling and backstepping control of the DFIG used in Wind Energy Conversion Systems. It focused on the evaluation of the proposed backstepping controller in terms of reference tracking and robustness against wind speed variations.
- B. Bossoufi *et al.* [17] proposed the backstepping adaptive control of the DFIG for variable speed WTs. This study presents a nonlinear backstepping controller that is designed using an adaptive pole placement strategy applied to WTs.

In this work we tried to combine all these studies mentioned to highlight the performances of both PI and backstepping controllers, in terms of robustness against wind speed variations and reference tracking in dynamic and steady states.

### 3. Wind turbine and DFIG modelling

As shown earlier in Fig. 1, the wind energy conversion system considered in our study is composed of a three-bladed horizontal-axis turbine and a DFIG generator, separated by a gear box system for speed adaptation.

In this adopted topology, the stator windings are directly connected to the grid and the rotor is connected to the grid through two power electronic converters, the RSC and GSC.

The model of both the mechanical and electrical parts is given below.

#### 3.1. Turbine model

The aerodynamic power of a turbine is written by Eq. (1) according to O. Barambones [14].

$$P_{\text{aero}} = C_p(\lambda, \beta) \frac{1}{2} \rho \pi R^2 v^3, \tag{1}$$

where  $C_p$  is the power coefficient that depends on the tip speed ratio  $\lambda$  and the pitch angle  $\beta$ . R is the blade radius and v is the wind speed.

The tip speed ratio  $\lambda$  is calculated by Eq. (2) [14].

$$\lambda = \frac{R\Omega_t}{v} \,, \tag{2}$$

where  $\Omega_t$  is the rotational speed of a turbine.

The expression of the power coefficient  $C_p$  of the turbine considered in this work is given by the following equation, (3).

$$C_p = 0.5176 \left( \frac{116}{\lambda_i} - 0.4\beta - 5 \right) e^{-\frac{21}{\lambda_i}} + 0.068\lambda,$$
 (3)

where:

$$\lambda_i = \frac{1}{\lambda + 0.08\beta} - \frac{0.035}{1 + \beta^3} \,. \tag{4}$$

#### 3.2. Gearbox model

The gear box system is modelled by the two equations bellow [15].

$$\begin{cases} \Omega_m = G \cdot \Omega_t \\ T_t = G \cdot T_m \end{cases}$$
 (5)

where: G is the gear ratio,  $\Omega_m$  and  $T_m$  are, respectively, the mechanical speed and the torque of the generator,  $\Omega_t$  and  $T_t$  are, respectively, the mechanical speed and the torque of the turbine.

The dynamic equation of the generator speed is given by the following equation, (6).

$$J\frac{\mathrm{d}\Omega_m}{\mathrm{d}t} = T_m - T_{em} - f\Omega_m\,,\tag{6}$$

where:  $T_{em}$  is the electromagnetic torque,  $f\Omega_m$  is the torque of viscous friction and J is the moment of inertia.

#### 3.3. DFIG Model

The dynamic model of the DFIG, adopted in this work, was built based on equations in the dq reference frame as indicated in the literature [10–12].

The rotor and stator voltages are illustrated by Eq. (7a) and the fluxes are given in the dq reference by Eq. (7b).

$$\begin{cases} V_{sd} = R_s i_{sd} + \frac{\mathrm{d}\phi_{sd}}{\mathrm{d}t} - \omega_s \phi_{sq} \\ V_{sq} = R_s i_{sq} + \frac{\mathrm{d}\phi_{sq}}{\mathrm{d}t} + \omega_s \phi_{sd} \\ V_{rd} = R_s i_{rd} + \frac{\mathrm{d}\phi_{rd}}{\mathrm{d}t} - \omega_r \phi_{rq} \\ V_{rq} = R_s i_{rq} + \frac{\mathrm{d}\phi_{rq}}{\mathrm{d}t} + \omega_r \phi_{rd} \end{cases}$$

$$(7a)$$

$$\begin{cases} \phi_{sd} = L_s i_{sd} + L_m i_{rd} \\ \phi_{sq} = L_s i_{sq} + L_m i_{rq} \\ \phi_{rd} = L_r i_{rd} + L_m i_{sd} \\ \phi_{rq} = L_r i_{rq} + L_m i_{sq} \end{cases}$$
(7b)

The active and reactive power are givens by the following equations, (8) and (9).

$$\begin{cases} P_s = V_{sd}i_{sd} + V_{sq}i_{sq} \\ Q_s = V_{sq}i_{sd} + V_{sd}i_{sq} \\ P_r = V_{rd}i_{rd} + V_{rq}i_{rq} \\ Q_r = V_{rq}i_{rd} + V_{rd}i_{rq} \end{cases}$$

$$(8)$$

The electromagnetic torque  $T_{em}$  is given by Eq. (9).

$$T_{em} = p \frac{L_m}{L_s} \left( \phi_{sq} i_{rd} - \phi_{sd} i_{rq} \right). \tag{9}$$

In order to achieve a vector control of active and reactive power, the stator field vector is oriented along the *d*-axis ( $\phi_{sd} = \phi_s$  and  $\phi_{sq} = 0$ ) [11, 13].

For simplification reasons, the stator resistance is considered negligible,  $R_s = 0$ .

Therefore, previous Eq. (7a) become Eq. (10).

$$\begin{cases} V_{sd} = 0 \\ V_{sq} = \omega_s \phi_s \end{cases}$$

$$\begin{cases} V_{rd} = R_r i_{rd} + L_r \sigma \frac{\mathrm{d}i_{rd}}{\mathrm{d}t} - g \omega_s L_r i_{rq} \\ V_{rq} = R_r i_{rq} + L_r \sigma \frac{\mathrm{d}i_{rq}}{\mathrm{d}t} - g \omega_s L_r i_{rq} + g \omega_s \frac{V_s L_m}{L_s \omega_s} \end{cases}$$

$$(10)$$

where  $\sigma = 1 - \frac{L_m^2}{L_s L_r}$ .

Therefore, the simplified expressions of the stator active and reactive power are given by Eq. (11).

$$\begin{cases} P_s = -\frac{V_s L_m}{L_s} i_{rq} \\ Q_s = -\frac{V_s L_m}{L_s} i_{rd} + \frac{V_s^2}{L_s \omega_s} \end{cases}$$
 (11)

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Thus, the electromagnetic torque is given by Eq. (12).

$$T_{em} = -p \frac{L_m}{L_s} \phi_s i_{rq} . {12}$$

## 4. PI controller design

In order to apply the PI control strategy for the RSC, the DFIG's model adopted previously in section 2 will be considered.

Considering the previous equations, (11) and (12), one can see that the control of the electromagnetic torque  $T_{em}$  is ensured by the quadrature component of the rotor current  $i_{rq}$  and the reactive power  $Q_s$  is controlled by the direct component  $i_{rd}$  in the dq reference frame.

Both the active power  $P_s$  or the electromagnetic torque  $T_{em}$  can be controlled. In both cases their references are obtained from the MPPT algorithm to guarantee the optimisation of the power captured by the WT.

The schematic diagram of the PI controller applied to the RSC is illustrated in Fig. 2.

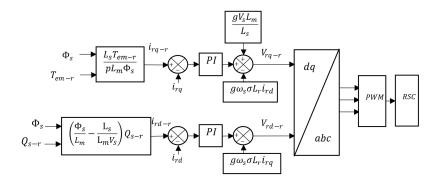


Fig. 2. Schematic diagram of the PI controller for RSC

The parameters of each PI controller applied are obtained based on the transfer function of the considered block. These parameters are determined using the pole compensation method in the closed loop. The structure of the PI controller including the transfer function of the rotor currents are given in Fig. 3.

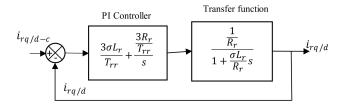


Fig. 3. Block diagram of PI controller of RSC

There,  $T_{rr}$  is the settling time of the rotor currents, and the parameters of the controller are chosen, as mentioned, by A.J. Laafou *et al.* [19].

In the same way, the structure of the schematic diagram of the PI controller for the GSC is illustrated in Fig. 4. Furthermore, the DC-link and grid current PI controllers applied to the GSC are illustrated in Fig. 5. As seen in the same figure, these two PI controllers are applied to the grid side, respectively, after developing the RL filter and DC link capacitor models.

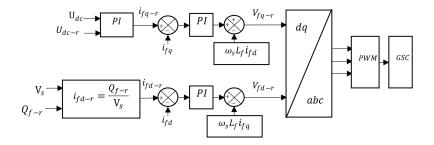


Fig. 4. Schematic diagram of PI control of GSC

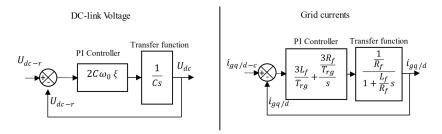


Fig. 5. PI controllers of the grid currents and DC-link voltage

Here,  $T_{rg}$  is the settling time of grid currents, and the parameters of the controller are chosen as in [19].

The parameters of this controller can be simplified as follows:

For rotor currents 
$$K_p^r = \frac{3\sigma L_r}{T_{rr}}$$
,  $K_i^r = \frac{3R_r}{T_{rr}}$ . (13)  
For grid currents  $K_p^r = \frac{3L_f}{T_{rg}}$ ,  $K_i^r = \frac{3R_f}{T_{rg}}$ . (14)  
For DC link voltage  $K_p^{dc} = 2C\omega_0\xi$ ,  $K_i^{dc} = \omega_0^2C = \frac{3}{\xi . T_{rdc}}$ . (15)

The setting values of these parameters are given in the Appendix.

#### 5. Backstepping controller design

#### 5.1. RSC control

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To design the backstepping controller for the RSC, the stator active and reactive power  $P_s$ and  $Q_s$  are provided by the following equations, (16) and (17), which have been derived from the DFIG model.

Active power 
$$\begin{cases} P_{s} = -\frac{V_{s}L_{m}}{L_{s}}i_{rq} \\ i_{rq} = \frac{1}{\sigma L_{r}} \left( V_{rq} - R_{r}i_{rq} - \sigma L_{r}\omega_{r}i_{rd} - g\frac{V_{s}L_{m}}{L_{s}} \right), \end{cases}$$
(16)
$$\begin{cases} Q_{s} = -\frac{V_{s}L_{m}}{L_{s}}i_{rd} + \frac{V_{s}^{2}}{L_{s}\omega_{s}} \\ i_{rd} = \frac{1}{\sigma L_{r}} \left( V_{rd} - R_{r}i_{rd} - \sigma L_{r}\omega_{r}i_{rq} \right). \end{cases}$$
(17)

Reactive power

These types of stator power are controlled by the rotor currents  $i_{rq}$  and  $i_{rd}$  with an intermediate virtual control  $v_{rq}$  and  $v_{rd}$ . Their reference values are determined following the recursive and sequential steps of backstepping control strategy based on the Lyapunov function [20]. Consequently, in order to achieve the stability of the system, the design of the backstepping controller can be carried out following two steps, as seen below. The current references (see Eq. 18) and the control voltages (see Eq. (24)) are computed, respectively, in the first and second step.

Step 1: Computation of current references:

Tracking errors:

$$\begin{cases} \varepsilon_1 = P_{s-c} - P_s \\ \varepsilon_3 = Q_{s-c} - Q_s \end{cases} \implies \begin{cases} \dot{\varepsilon}_1 = \dot{P}_{s-c} - \dot{P}_s \\ \dot{\varepsilon}_3 = \dot{Q}_{s-c} - \dot{Q}_s \end{cases}$$
 (18)

Lyapunov functions:

$$V_1 = \frac{1}{2}\varepsilon_1^2, \quad V_3 = \frac{1}{2}\varepsilon_3^2.$$
 (19)

(17)

Derivatives of Lyapunov functions:

$$\begin{cases}
\dot{V}_1 = \varepsilon_1 \dot{\varepsilon}_1 = \varepsilon_1 \left[ \dot{P}_{s-c} - A_1 \left( V_{rq} - R_r i_{rq} - A_2 i_{rd} - A_3 \right) \right] \\
\dot{V}_3 = \varepsilon_3 \dot{\varepsilon}_3 = \varepsilon_3 \left[ \dot{Q}_{s-c} - A_1 \left( V_{rd} - R_r i_{rd} + A_2 i_{rq} \right) \right]
\end{cases}, (20)$$

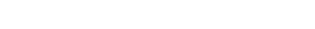
where:

$$A_1 = \frac{V_s L_m}{L_s \sigma L_r} \; , \quad A_2 = \sigma L_r \omega_r \; , \quad A_3 = g \frac{V_s L_m}{L_s} \; . \label{eq:A1}$$

Rotor currents as virtual commands:

$$i_{rq-c} = \frac{1}{A_1 R_r} \left[ \dot{P}_{s-c} + c_1 \varepsilon_1 \right] - \frac{1}{R_r} \left( V_{rq} - A_2 i_{rd} - A_3 \right),$$

$$i_{rd-c} = \frac{1}{A_1 R_r} \left[ \dot{Q}_{s-c} + c_3 \varepsilon_3 \right] - \frac{1}{R_r} \left( V_{rd} + A_2 i_{rq} \right).$$
(21)



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Step 2: Computation of control voltages:

Tracking errors:

$$\begin{cases} \varepsilon_2 = i_{rq-c} - i_{rq} \\ \varepsilon_4 = i_{rd-c} - i_{rd} \end{cases} \implies \begin{cases} \dot{\varepsilon}_2 = i_{rq-c} - i_{rq} \\ \dot{\varepsilon}_4 = i_{rd-c} - i_{rd} \end{cases}$$
 (22)

Lyapunov functions:

$$V_2 = \frac{1}{2}\varepsilon_1^2 + \frac{1}{2}\varepsilon_2^2, \quad V_4 = \frac{1}{2}\varepsilon_3^2 + \frac{1}{2}\varepsilon_4^2.$$
 (23)

Derivatives Lyapunov functions:

$$\begin{cases} \dot{V}_2 = \varepsilon_1 \dot{\varepsilon}_1 + \varepsilon_2 \dot{\varepsilon}_2 \\ \dot{V}_4 = \varepsilon_3 \dot{\varepsilon}_3 + \varepsilon_4 \dot{\varepsilon}_4 \end{cases}$$
(24)

Therefore:

$$\begin{cases} \dot{V}_{2} = \varepsilon_{1} \left[ \dot{P}_{s-c} - A_{1} \left( V_{rq} - R_{r} \left( i_{rq-c} - \varepsilon_{2} \right) - A_{2} i_{rd} - A_{3} \right) \right] \\ + \varepsilon_{2} \left[ \dot{i}_{rq-c} - \frac{1}{\sigma L_{r}} \left( V_{rq} - R_{r} \left( i_{rq-c} - \varepsilon_{2} \right) - A_{2} i_{rd} - A_{3} \right) \right] \\ \dot{V}_{4} = \varepsilon_{3} \left[ \dot{Q}_{s-c} - A_{1} \left( V_{rd} - R_{r} \left( i_{rd-c} - \varepsilon_{4} \right) + A_{2} i_{rq} \right) \right] \\ + \varepsilon_{4} \left[ \dot{i}_{rd-c} - A_{1} \left( V_{rd} - R_{r} \left( i_{rd-c} - \varepsilon_{4} \right) - A_{2} i_{rq} \right) \right] \end{cases}$$
(25)

Finally, we will have to choose the references of rotor voltages as the actually accessible commands. Their reference values should guarantee that the derivatives of Lyapunov functions are negative as expressed by Eq. (26).

$$\dot{V}_2 = -c_1 \varepsilon_1^2 - c_2 \varepsilon_2^2 < 0, \quad \dot{V}_4 = -c_3 \varepsilon_3^2 - c_4 \varepsilon_4^2 < 0, \tag{26}$$

where  $c_1, c_2, c_3$  and  $c_4$  are positive parameters that we must choose properly to ensure asymptotic convergence stability according to the Lyapunov theory [17].

In our simulation model we chose them as,  $c_1 = 80\,000$ ,  $c_2 = 5\,000$ ,  $c_3 = 9\,000$  and  $c_4 = 6\,000$  [17].

Therefore, the control voltages are given by Eq. (27).

$$\begin{cases} V_{rq-c} = \frac{1}{\sigma L_r} \left[ -c_2 \varepsilon_2 - \dot{i}_{rq-c} + A_1 R_r \varepsilon_1 \right] + B_1 \\ V_{rd-c} = \frac{1}{\sigma L_r} \left[ -c_4 \varepsilon_4 - \dot{i}_{rd-c} + A_1 R_r \varepsilon_3 \right] + B_2 \end{cases}$$
(27)

where:

$$B_1 = -R_r (i_{rq-c} - \varepsilon_2) - A_2 i_{rd} - A_3$$
 and  $B_2 = -R_r (i_{rd-c} - \varepsilon_4) + A_2 i_{rq}$ .

The block diagram of the backstepping controller applied to the RSC is presented in Fig. 6. In this diagram all the steps, previously mentioned, that are required to turn out the control law of the rotor voltages are illustrated.

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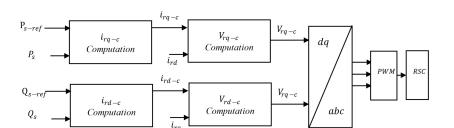


Fig. 6. Backstepping control diagram applied to the RSC

#### 5.2. GSC control

For the control of the GSC, we consider the model of the RL filter, which is defined by equations of the rotor active and reactive power, (28) and (29).

Active power 
$$\begin{cases} \dot{P}_{f} = \frac{V_{s}}{L_{f}} \left( V_{fq} - R_{f} i_{fq} - L_{f} \omega_{s} i_{fd} - V_{s} \right) \\ \dot{i}_{fq} = \frac{1}{L_{f}} \left( V_{fq} - R_{f} i_{fq} - L_{f} \omega_{s} i_{fd} - V_{s} \right) \end{cases}$$

$$\begin{cases} \dot{Q}_{f} = \frac{V_{s}}{L_{f}} \left( V_{fd} - R_{f} i_{fd} - L_{f} \omega_{s} i_{fq} - V_{s} \right) \\ \dot{i}_{fd} = \frac{1}{L_{f}} \left( V_{fd} - R_{f} i_{fd} - L_{f} \omega_{s} i_{fq} - V_{s} \right) \end{cases}$$

$$(28)$$
Reactive power

By following the same backstepping strategy detailed earlier in RSC control according to the use of Lyapunov functions, the expressions of the filter current reference Eq. (30) of  $i_{fq}$  and  $i_{fd}$ are given in the first step, while voltage reference Eq. (31),  $V_{fd}$  and  $V_{fq}$ , are given in the second step.

Therefore:

Grid current references: 
$$\begin{cases} i_{f\,q-c} = \frac{1}{R_f} \left[ \frac{L_f}{V_s} \left( \dot{P}_{f-c} + k_1 \varepsilon_1 \right) + \left( V_{f\,q} - L_f \, \omega_s i_{f\,d} - V_s \right) \right] \\ i_{f\,d-c} = \frac{1}{R_f} \left[ \frac{L_f}{V_s} \left( \dot{Q}_{s-c} + k_3 \varepsilon_3 \right) + \left( V_{f\,d} - L_f \, \omega_s i_{f\,q} \right) \right] \end{cases}, \tag{30}$$

Voltages references: 
$$\begin{cases} V_{f\,q-c} = L_f \left( -k_2 \varepsilon_2 - \dot{i}_{f\,q-c} + \frac{V_s}{L_f} \varepsilon_1 \right) - \left( R_f i_{f\,q} + L_f \omega_s i_{f\,d} + V_s \right) \\ V_{f\,d-c} = L_f \left( -k_4 \varepsilon_4 - \dot{i}_{f\,d-c} + \frac{V_s}{L_f} \varepsilon_3 \right) - \left( R_f i_{f\,d} - L_f \omega_s i_{f\,q} \right) \end{cases} . \tag{31}$$

In the same way as PI controllers for the RSC, the parameters  $k_1$ ,  $k_2$ ,  $k_3$  and  $k_4$  are positive parameters chosen properly to guarantee the asymptotic convergence stability according to the Lyapunov theory. According to Y. Moumani et al. [17], they are chosen in this proposed model to be

$$k_1 = 10\,000$$
,  $k_2 = 80\,000$ ,  $k_3 = 20\,000$  and  $k_4 = 6\,000$ .

Based on Eqs. (28) and (29), the block diagram of the backstepping controller applied to the GSC is given in Fig. 7.

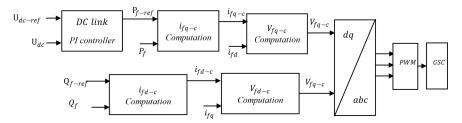


Fig. 7. Block diagram of backstepping controller applied to the GSC

#### 6. Simulation results

To validate the performance of the proposed PI and backstepping controllers, MATLAB/ Simulink software has been used to build the model of the entire WECS including the turbine and the DFIG.

After designing the two controllers, the simulation scenario adopted is based on a wind speed profile as a signal of sudden changes in wind speed, as illustrated in Fig. 8 allows one to test tracking speed as well as tracking error in both transient and steady states.

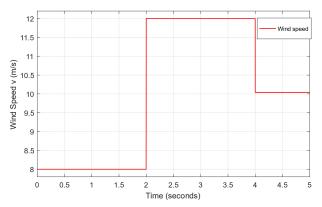


Fig. 8. Form of applied wind speed profile

The obtained results for the stator active and reactive power are presented respectively in Fig. 9 and Fig. 10. From these figures, one can see obviously that the outputs  $P_s$  and  $Q_s$  converge perfectly to their references when there is a random sudden change of wind speed. The value of  $P_s$  is negative because DFIG works as a generator.

The active power  $P_s$  converges to its reference value  $P_{s-ref}$  determined by an MPPT algorithm and the reactive power is kept at zero to ensure a unitary power factor [21]. This means that all the tracking errors converge to zero. That proves the effectiveness of the two controllers, but

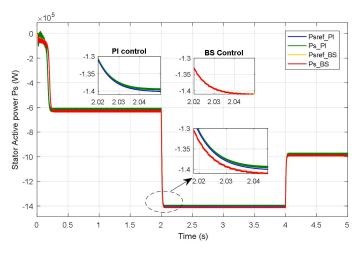


Fig. 9. Stator active power for PI and BS control

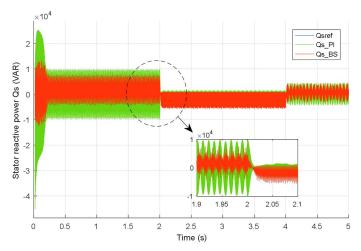


Fig. 10. Stator reactive power for PI and BS control

backstepping is quite more effective than PI when it comes to error cancellation in both transient and steady states.

Fig. 11 shows the evolution of the power factor  $C_p$  that depends on wind speed. In this figure, one can see that the power coefficient is kept at its optimal value despite the disturbance caused by the sudden changes in wind speed. The principal observed advantage here is that the backstepping controller response is much faster than that of the PI controller.

Fig. 12, which illustrates the DC link voltage for both PI and backstepping controllers, shows that there is overshooting in the PI control strategy, the voltage value exceeds its reference value while trying to stabilise against wind speed changes.

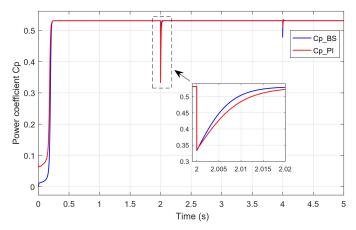


Fig. 11. Power coefficient  $C_p$ 

Apparently, the same previous observations regarding the settling time are also noticed in Fig. 12. The voltage  $U_{dc}$  follows its reference with a very small settling time which means that is much faster compared to PI.

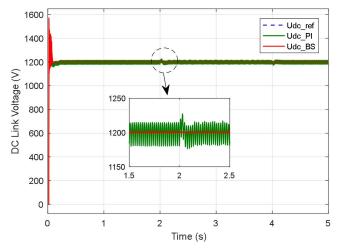
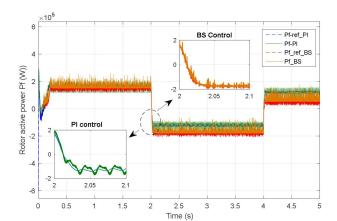


Fig. 12. DC-Link voltage  $U_{dc}$ 

Figures 13 and 14 present, respectively, the rotor active and reactive power for both PI and backstepping controllers. From Fig. 13 one can notices that the power  $P_f$  is negative between 2 s and 4 s. It means that the DFIG works in hypersynchronous mode, which is obvious since the rotor speed exceeds its nominal value. Whereas the reactive power of the rotor is kept at zero, to ensure a unitary power factor, as illustrated by Fig. 14.



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Fig. 13. Rotor active power  $P_f$ 

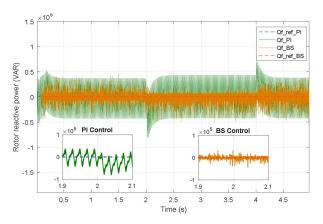


Fig. 14. Rotor reactive power  $Q_f$ 

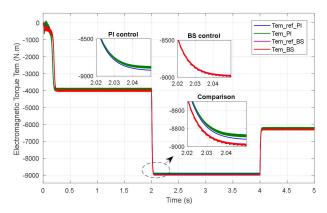


Fig. 15. Electromagnetic torque  $T_{em}$  (N·m)

For both controls, the electromagnetic torque  $T_{em}$  is illustrated by the following Figure 15, it has exactly the same form of active power which affirms the same differences discussed earlier between PI and backstepping.

### 7. Conclusion

In this paper a comparative study between two control strategies was given. The studied controllers are the conventional PI control and an advanced non-linear approach known as back-stepping control. These two strategies, to control a WT-driven DFIG, are applied to two converters, the RSC and GSC, leading to the optimization of the power captured by the WT.

The obtained results carried out from this study have proved that both controllers show quite satisfying performances, but the backstepping technique is more effective in terms of robustness against disturbances such as wind speed variations.

Moreover, the non-linearity of the backstepping makes the system more stable and much faster than its competitor due to its short settling time which proves its capability to cancel the tracking errors in a very short time.

However, the simplicity and the low cost of the classical PI controller make it still the most employed controller compared to the backstepping controller which is more complex, and more sensors are needed for its implementation.

In future work, a hardware implementation, as well as a further study, should be carried on in order to test the performances of the proposed controllers against voltage dips expected in the terminals of the wind power system.

#### Nomenclature

| $P_{\rm aero}$ : | The aerodynamic power of wind turbine (W)       | $V_{rd}$ :    | direct component of $V_r$ in $dq$ reference     |
|------------------|---|---------------|---|
| $T_t$ :          | Wind turbine torque (N.m)                       | $V_{rq}$ :    | quadrature component of $V_r$ in $dq$ reference |
| v:               | Wind speed (m/s)                                | $i_{sd}$ :    | direct component of stator current              |
| R:               | Blade radius (m)                                | $i_{Sq}$ :    | quadrature component of stator current          |
| $\lambda$ :      | Tip speed ratio                                 | $\phi_{sd}$ : | direct component of stator flux                 |
| G:               | Gearbox ratio                                   | $\phi_{Sq}$ : | quadrature component of stator flux             |
| $\Omega_m$ :     | mechanical speed of the generator (rad/s)       | $i_{rd}$ :    | direct component of rotor current               |
| $T_m$ :          | mechanical torque of the generator (N.m)        | $i_{rq}$ :    | quadrature component of rotor current           |
| f:               | Damping coefficient                             | $P_s$ :       | Stator active power                             |
| p:               | number of pair poles                            | $Q_s$ :       | stator reactive power                           |
| J:               | Moment of inertia                               | $i_{fd}$ :    | direct component of grid current                |
| $T_{em}$ :       | Electromagenetic torque (N.m)                   | $i_{fq}$ :    | quadrature component of grid current            |
| $V_s$ :          | Stator voltage (V)                              | $P_f$ :       | rotor active power                              |
| $V_r$ :          | rotor voltage (V)                               | $i_{sd}$ :    | direct component of stator current              |
| $V_{sd}$ :       | direct component of $V_s$ in $dq$ reference     | $i_{SQ}$ :    | quadrature component of stator current          |
| $V_{sq}$ :       | quadrature component of $V_s$ in $dq$ reference |               |   |

#### **Appendix**

The WECS parameters used for the simulation are given in Tables 1, 2, 3 and 4.

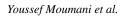


Table 1. DFIG parameters

| Parameter name            | Symbol        | Value  | Unit |
|---------------------------|---------------|--------|------|
| Rated power               | $P_n$         | 1.5    | MW   |
| Rated voltage             | $U_n$         | 690    | V    |
| Nominal frequency         | f             | 50     | Hz   |
| Rated rotor speed         | N             | 1750   | rpm  |
| number of pole pairs      | p             | 2      |      |
| Stator resistance         | $R_S$         | 2.65   | mΩ   |
| rotor resistance          | $R_r$         | 2.63   | mΩ   |
| stator leakage inductance | $L_{s\sigma}$ | 0.1687 | mH   |
| rotor leakage inductance  | $L_{r\sigma}$ | 0.1337 | mH   |
| magnetizing inductance    | $L_m$         | 5.4749 | mH   |

Table 2. The parameters of the turbine

| Parameter name   | Symbol | Value | Unit              |
|------------------|--------|-------|-------------------|
| Rated power      | $P_n$  | 1.5   | MW                |
| Rated wind speed | v      | 13    | m/s               |
| Density of air   | ρ      | 1,225 | kg/m <sup>3</sup> |
| Blade radius     | R      | 30    | m                 |
| Gearbox ratio    | G      | 55    |                   |

Table 3. Parameters of the grid side

| Parameter name    | Symbol   | Value    | Unit |
|-------------------|----------|----------|------|
| DC-link voltage   | $U_{dc}$ | 1 200    | V    |
| DC-link capacitor | С        | 10 028.7 | μF   |
| filter resistance | $R_f$    | 0.3174   | Ω    |
| filter inductance | $L_f$    | 3.0103   | mH   |

Table 4. Controller parameters

| Parameter name      | Symbol     | Value    |
|---------------------|------------|----------|
| For rotor currents  | $K_p^r$    | 0.8921   |
| roi rotor currents  | $K_i^r$    | 7.8900   |
| Ean anid assessants | $K_p^g$    | 9.0309   |
| For grid currents   | $K_i^g$    | 105.4380 |
| For DC link voltage | $K_p^{DC}$ | 1.0029   |
| For DC link voltage | $K_i^{DC}$ | 50.1586  |

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